

NOTE ON CERTAIN OPERATORS OF JACOBI FORMS OF
HALF INTEGRAL WEIGHT

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Abstract: In this note we characterise two operators I_m and K_m on the space of Jacobi forms of half-integral weight.

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1. Introduction

In this note, we characterise certain operators I_m and K_m on the space of Jacobi forms of weight $k + 1/2$ ($k > 1$ is an integer), index m and level 4. The operator I_m has been introduced in [2] and proved that it maps Jacobi forms of weight $k + 1/2$, index m , level 4 into the space of Jacobi forms of weight $k + 1/2$, index 1, level $4m$ and character χ_m - a real character mod m or $4m$ according as $m \equiv 1 \pmod{4}$ or $m \equiv 2, 3 \pmod{4}$. It is also known that, the operator I_m preserves the space of cusp forms. It has a connection with the Eichler-Zagier maps: $\phi|Z_m := \phi|I_m Z_1$ where ϕ is a Jacobi form of weight $k + 1/2$, index m , level 4 and Z_m is the Eichler-Zagier map as in [2]. We first prove that the index changing operator I_m preserves the